



Two's Complement
Negative Numbers
Floating Point Notation
Mantissa & Exponent

NATIONAL 5 BINARY

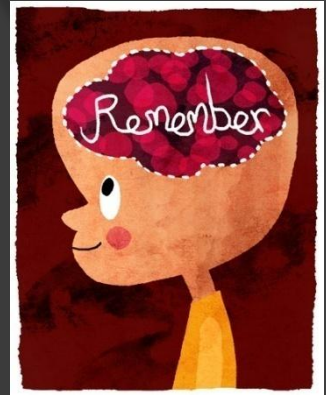
Two's Complement

- ⦿ This is the name given to binary system we use to represent **negative** numbers.
- ⦿ The first bit used in two's complement is **-128** instead of 128 we usually have:

-128 64 32 16 8 4 2 1

Note!!

- If you are given a two's complement question which begins with a '1' then your answer will be **negative**
- If you are given two's complement question which begins with a '0' then your answer will be **positive**



Negative Numbers

- For example the number -45 is represented by 11010011 in two's complement

<u>-128</u>	<u>64</u>	<u>32</u>	<u>16</u>	<u>8</u>	<u>4</u>	<u>2</u>	<u>1</u>
1	1	0	1	0	0	1	1

$$= -128 + 64 + 16 + 2 + 1 = -45$$

Negative Numbers

- For example the number -81 is represented by 10101111 in two's complement

<u>-128</u>	<u>64</u>	<u>32</u>	<u>16</u>	<u>8</u>	<u>4</u>	<u>2</u>	<u>1</u>
1	0	1	0	1	1	1	1

$$= -128 + 32 + 8 + 4 + 2 + 1 = -81$$

Floating Point Notation

- ⦿ This is the name given to the binary system used to represent numbers with a **decimal point**.

- ⦿ For example :
 - 33.9
 - 0.0056
 - 1289.1285

Mantissa & Exponent

⦿ A floating point number is made up of:

- Mantissa : the 'fraction' part
- Exponent : the 'power of' part

⦿ For example:

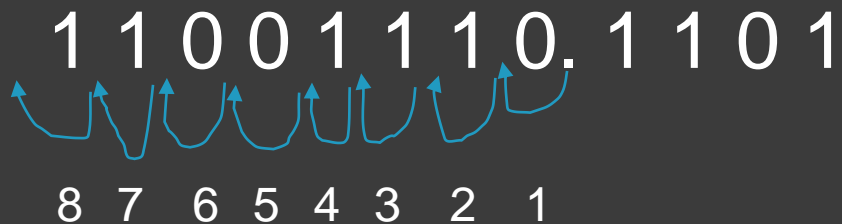
$$100111.10100 = 10011110100 \times 2^{0110}$$

Mantissa

Exponent

Example

11001110.1101



Step 1 – count out how many steps until the decimal point is out of the number

110011101101 x 2⁸

Step 2 – write out your number without the decimal point x 2 to the power of how many steps it took to remove the decimal point

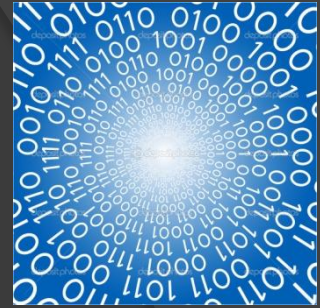
110011101101 x 2¹⁰⁰⁰

Step 3 – rewrite the power of as a binary number as the computer does not understand an '8'

Floating Point Notation

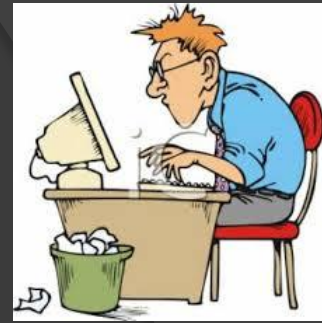
- ◎ The **accuracy** of a floating point number is increased by allocating more bits to the **mantissa**.
- ◎ The **range** of numbers that can be stored is increased by allocating more bits to the **exponent**.

Examples



- ⦿ A floating point number which uses 16 bits for the mantissa and 8 bits for the exponent is **less accurate and stores a smaller range of numbers** than a floating point number that uses 24 bits for the mantissa and 16 bits for the exponent.

Question



- Jonathan needs to store the floating point numbers accurately in his program.

Which option should he use and why?

Option 1 16-bit exponent 16-bit mantissa

Option 2 8-bit exponent 24-bit mantissa